

The Portable Extensible Toolkit for Scientific Computing

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assess solver performance,
and optimize solvers
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Outline

- 1 Controlling the Solver
- 2 Where do I begin?
- 3 How do I improve?
- 4 Debugging
- 5 Examples

Controlling PETSc

All of PETSc can be controlled by **options**

```
-ksp_type gmres
```

```
-start_in_debugger
```

All objects can have a prefix, `-velocity_pc_type jacobi`

All PETSc options can be namespaced

```
-sub_ksp_type bicg
```

```
-fieldsplit_1_pc_type jacobi
```

Controlling PETSc

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```
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Examples

We will illustrate options using

PETSc SNES **ex5**, located at
`$PETSC_DIR/src/snes/examples/tutorials/ex5.c`

and

PETSc SNES **ex62**, located at
`$PETSC_DIR/src/snes/examples/tutorials/ex62.c`

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Nonlinear Systems

I am not going to discuss
nonlinear systems today,

however if Newton is failing,

contact

petsc-maint@mcs.anl.gov

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What is a Krylov solver?

A Krylov solver builds a small model of a linear operator A , using a subspace defined by

$$\mathcal{K}(A, r) = \text{span}\{r, Ar, A^2r, A^3r, \dots\}$$

where r is the initial residual.

The small system is solved directly, and the solution is projected back to the original space.

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What Should I Know About Krylov Solvers?

- They can handle *low-mode* errors
- They need preconditioners
- They do a lot of inner products

What is a Preconditioner?

A preconditioner M changes a linear system,

$$M^{-1}Ax = M^{-1}b$$

so that the effective operator is $M^{-1}A$, which is hopefully **better** for Krylov methods.

- Preconditioner should be inexpensive
- Preconditioner should accelerate convergence

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Always start with LU

Always, always start with LU:

- No iterative tolerance
- (Almost) no condition number dependence
- Check for accidental singularity

In parallel, you need a 3rd party package

- MUMPS (`--download-mumps`)
- SuperLU (`--download-superlu_dist`)

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What if LU fails?

LU will fail for

- Singular problems
- Saddle-point problems

For saddles use `PC_FIELDSPLIT`

- Separately solves each field
- Decomposition is automatic in PyLith
- Autodetect with `-pc_fieldsplit_detect_saddle_point`
- Exact with full Schur complement solve

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 - Back off in steps

What solver did you use?

Use `-snes_view` or `-ksp_view` to output a description of the solver:

```
KSP Object:          (fieldsplit_0_)          1 MPI processes
type: fgmres
  GMRES: restart=100, using Classical (unmodified) Gram-
        Schmidt Orthogonalization with no iterative refinemen
  GMRES: happy breakdown tolerance 1e-30
maximum iterations=1, initial guess is zero
tolerances:  relative=1e-09, absolute=1e-50,
             divergence=10000
right preconditioning
has attached null space
using UNPRECONDITIONED norm type for convergence test
```


What did the convergence look like?

Use `-snes_monitor` and `-ksp_monitor`, or `-log_summary`:

What did the convergence look like?

Use `-snes_monitor` and `-ksp_monitor`, or `-log_summary`:

```
0 SNES Function norm 0.207564
1 SNES Function norm 0.0148968
2 SNES Function norm 0.000113968
3 SNES Function norm 6.9256e-09
4 SNES Function norm < 1.e-11
```

What did the convergence look like?

Use `-snes_monitor` and `-ksp_monitor`, or `-log_summary`:

```
0 KSP Residual norm 1.61409
  Residual norms for mg_levels_1_ solve.
  0 KSP Residual norm 0.213376
  1 KSP Residual norm 0.0192085
Residual norms for mg_levels_2_ solve.
0 KSP Residual norm 0.223226
1 KSP Residual norm 0.0219992
  Residual norms for mg_levels_1_ solve.
  0 KSP Residual norm 0.0248252
  1 KSP Residual norm 0.0153432
Residual norms for mg_levels_2_ solve.
0 KSP Residual norm 0.0124024
1 KSP Residual norm 0.0018736
1 KSP Residual norm 0.02282
```

What did the convergence look like?

Use `-snes_monitor` and `-ksp_monitor`, or `-log_summary`:

Event	Count		Time (sec)		Flops		Total
	Max	Ratio	Max	Ratio	Max	Ratio	Mflop/s
KSPSetUp	12	1.0	3.6259e-03	1.0	0.00e+00	0.0	0
KSPSolve	3	1.0	4.8937e-01	1.0	8.93e+05	1.0	2
SNESolve	1	1.0	4.9477e-01	1.0	9.22e+05	1.0	2

Look at timing

Use `-log_summary`:

Event	Time (sec)		Flops		--- Global ---					Total MF/s
	Max	Ratio	Max	Ratio	%T	%f	%M	%L	%R	
VecMDot	1.8904e-03	1.0	2.49e+04	1.0	0	3	0	0	0	13
MatMult	2.1026e-03	1.0	2.65e+05	1.0	0	29	0	0	0	126
PCApply	4.6001e-01	1.0	7.78e+05	1.0	58	84	0	0	64	2
KSPSetUp	3.6259e-03	1.0	0.00e+00	0.0	0	0	0	0	4	0
KSPSolve	4.8937e-01	1.0	8.93e+05	1.0	61	97	0	0	90	2
SNESolve	4.9477e-01	1.0	9.22e+05	1.0	62	100	0	0	92	2

Use `-log_summary_python` to get this information as a Python module

Look at timing

Use `-log_summary`:

Event	Time (sec)		Flops		--- Global ---					Total MF/s
	Max	Ratio	Max	Ratio	%T	%f	%M	%L	%R	
VecMDot	1.8904e-03	1.0	2.49e+04	1.0	0	3	0	0	0	13
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KSPSetUp	3.6259e-03	1.0	0.00e+00	0.0	0	0	0	0	4	0
KSPSolve	4.8937e-01	1.0	8.93e+05	1.0	61	97	0	0	90	2
SNESolve	4.9477e-01	1.0	9.22e+05	1.0	62	100	0	0	92	2

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-
-
- 3 How do I improve?**
 - Look at what you have
 - **Back off in steps**

Weaken the KSP

GMRES \implies BiCGStab

- `-ksp_type bcgs`
- Less storage
- Fewer dot products (less work)
- Variants `-ksp_type bcgs1` and `-ksp_type ibcgs`

Complete **Table** of Solvers and Preconditioners

Weaken the PC

LU \implies ILU

- `-pc_type ilu`
- **Less storage and work**

In parallel,

- `Hypre -pc_type hypre -pc_hypre_type euclid`
- `Block-Jacobi -pc_type bjacobi -sub_pc_type ilu`
- `Additive Schwarz -pc_type asm -sub_pc_type ilu`

Default for MG smoother is Chebychev/SOR(2)

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Default for MG smoother is Chebychev/SOR(2)

Algebraic Multigrid (AMG)

- Can solve elliptic problems
 - Laplace, elasticity, Stokes
- Works for unstructured meshes
- `-pc_type gamg, -pc_type ml,`
`-pc_type hypre -pc_hypre_type boomeramg`
- **CRUCIAL** to have an accurate near-null space
 - `MatSetNearNullSpace()`
 - PyLith provides this automatically
- Use `-pc_mg_log` to put timing in its own log stage

PC_FieldSplit

- **Separate solves for block operators**
 - Physical insight for subsystems
 - Have optimal PCs for simpler equations
 - Suboptions `fs_fieldsplit_0_*`
- **Flexibly combine subsolves**
 - Jacobi: `fs_pc_fieldsplit_type = additive`
 - Gauss-Siedel: `fs_pc_fieldsplit_type = multiplicative`
 - Schur complement: `fs_pc_fieldsplit_type = schur`

Stokes example

The common block preconditioners for Stokes require only options:

The Stokes System

$$\begin{pmatrix} A & B \\ B^T & 0 \end{pmatrix}$$

Stokes example

The common block preconditioners for Stokes require only options:

```
-pc_type fieldsplit
-pc_field_split_type additive
-fieldsplit_0_pc_type ml
-fieldsplit_0_ksp_type preonly
-fieldsplit_1_pc_type jacobi
-fieldsplit_1_ksp_type preonly
```

$$\text{PC} \begin{pmatrix} \hat{A} & 0 \\ 0 & I \end{pmatrix}$$

Cohouet & Chabard, Some fast 3D finite element solvers for the generalized Stokes problem, 1988.

Stokes example

The common block preconditioners for Stokes require only options:

```
-pc_type fieldsplit
-pc_field_split_type multiplic
-fieldsplit_0_pc_type hypre
-fieldsplit_0_ksp_type preonly
-fieldsplit_1_pc_type jacobi
-fieldsplit_1_ksp_type preonly
```

$$PC \begin{pmatrix} \hat{A} & B \\ 0 & I \end{pmatrix}$$

Elman, Multigrid and Krylov subspace methods for the discrete Stokes equations, 1994.

Stokes example

The common block preconditioners for Stokes require only options:

```
-pc_type fieldsplit
-pc_field_split_type schur
-fieldsplit_0_pc_type gamg
-fieldsplit_0_ksp_type preonly
-fieldsplit_1_pc_type none
-fieldsplit_1_ksp_type minres

-pc_fieldsplit_schur_factorization_type diag
```

$$\text{PC} \begin{pmatrix} \hat{A} & 0 \\ 0 & -\hat{S} \end{pmatrix}$$

May and Moresi, Preconditioned iterative methods for Stokes flow problems arising in computational geodynamics, 2007.

Olshanskii, Peters, and Reusken, Uniform preconditioners for a parameter dependent saddle point problem with application to generalized Stokes interface equations, 2006.

Stokes example

The common block preconditioners for Stokes require only options:

```
-pc_type fieldsplit
-pc_field_split_type schur
-fieldsplit_0_pc_type gamg
-fieldsplit_0_ksp_type preonly
-fieldsplit_1_pc_type none
-fieldsplit_1_ksp_type minres

-pc_fieldsplit_schur_factorization_type lower
```

$$\text{PC} \begin{pmatrix} \hat{A} & 0 \\ B^T & \hat{S} \end{pmatrix}$$

May and Moresi, Preconditioned iterative methods for Stokes flow problems arising in computational geodynamics, 2007.

Stokes example

The common block preconditioners for Stokes require only options:

```
-pc_type fieldsplit
-pc_field_split_type schur
-fieldsplit_0_pc_type gamg
-fieldsplit_0_ksp_type preonly
-fieldsplit_1_pc_type none
-fieldsplit_1_ksp_type minres

-pc_fieldsplit_schur_factorization_type upper
```

$$\text{PC} \begin{pmatrix} \hat{A} & B \\ 0 & \hat{S} \end{pmatrix}$$

May and Moresi, Preconditioned iterative methods for Stokes flow problems arising in computational geodynamics, 2007.

Stokes example

The common block preconditioners for Stokes require only options:

```
-pc_type fieldsplit
-pc_field_split_type schur
-fieldsplit_0_pc_type gamg
-fieldsplit_0_ksp_type preonly
-fieldsplit_1_pc_type lsc
-fieldsplit_1_ksp_type minres

-pc_fieldsplit_schur_factorization_type upper
```

$$\text{PC} \begin{pmatrix} \hat{A} & B \\ 0 & \hat{S}_{\text{LSC}} \end{pmatrix}$$

May and Moresi, Preconditioned iterative methods for Stokes flow problems arising in computational geodynamics, 2007.

Kay, Loghin and Wathen, A Preconditioner for the Steady-State N-S Equations, 2002.

Elman, Howle, Shadid, Shuttleworth, and Tuminaro, Block preconditioners based on approximate commutators, 2006.

Stokes example

The common block preconditioners for Stokes require only options:

```
-pc_type fieldsplit
-pc_field_split_type schur
-pc_fieldsplit_schur_factorization_type full
```

PC

$$\begin{pmatrix} I & 0 \\ B^T A^{-1} & I \end{pmatrix} \begin{pmatrix} \hat{A} & 0 \\ 0 & \hat{S} \end{pmatrix} \begin{pmatrix} I & A^{-1} B \\ 0 & I \end{pmatrix}$$

Why us FGMRES?

Flexible GMRES (FGMRES) allows a **different preconditioner** at each step:

- Takes twice the memory
- Needed for iterative PCs
- Avoided sometimes with a careful PC choice

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Correctness Debugging

- Automatic generation of tracebacks
- Detecting memory corruption and leaks
- Optional user-defined error handlers

Interacting with the Debugger

- Launch the debugger
 - `-start_in_debugger [gdb,dbx,noxterm]`
 - `-on_error_attach_debugger [gdb,dbx,noxterm]`
- Attach the debugger only to some parallel processes
 - `-debugger_nodes 0,1`
- Set the display (often necessary on a cluster)
 - `-display khan.mcs.anl.gov:0.0`

Debugging Tips

- Put a breakpoint in `PetscError()` to catch errors as they occur
- PETSc tracks memory overwrites at both ends of arrays
 - The `CHKMEMQ` macro causes a check of all allocated memory
 - Track memory overwrites by bracketing them with `CHKMEMQ`
- PETSc checks for leaked memory
 - Use `PetscMalloc()` and `PetscFree()` for all allocation
 - Print unfreed memory on `PetscFinalize()` with `-malloc_dump`
- Simply the best tool today is **valgrind**
 - It checks memory access, cache performance, memory usage, etc.
 - <http://www.valgrind.org>
 - Need `-trace-children=yes` when running under MPI

Outline

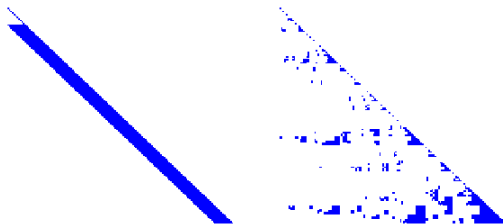
- 1 Controlling the Solver
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Try it out

- ```
$ cd $PETSC_DIR/src/snes/examples/tutorials && make ex5
```
- `$ ./ex5 -da_grid_x 10 -da_grid_y 10 -par 6.7 -snes_monitor -{ksp,snes}_converged_reason -snes_view`
  - `$ ./ex5 -da_grid_x 10 -da_grid_y 10 -par 6.7 -snes_monitor -{ksp,snes}_converged_reason -snes_view -mat_view_draw -draw_pause 0.5`
  - `$ ./ex5 -da_grid_x 10 -da_grid_y 10 -par 6.7 -snes_monitor -{ksp,snes}_converged_reason -snes_view -mat_view_draw -draw_pause 0.5 -pc_type lu -pc_factor_mat_ordering_type natural`
  - **Use `-help` to find other ordering types**

# Sample output

```
0 SNES Function norm 1.139460779565e+00
Linear solve converged due to CONVERGED_RTOL iterations 1
1 SNES Function norm 4.144493702305e-02
Linear solve converged due to CONVERGED_RTOL iterations 1
2 SNES Function norm 6.309075568032e-03
Linear solve converged due to CONVERGED_RTOL iterations 1
3 SNES Function norm 3.359792279909e-04
Linear solve converged due to CONVERGED_RTOL iterations 1
4 SNES Function norm 1.198827244256e-06
Linear solve converged due to CONVERGED_RTOL iterations 1
5 SNES Function norm 1.545029314765e-11
```



# Sample output (SNES and KSP)

SNES Object: 1 MPI processes

type: ls

line search variant: CUBIC

alpha=1.000000000000e-04, maxstep=1.000000000000e+08, minlambda

damping factor=1.000000000000e+00

maximum iterations=50, maximum function evaluations=10000

tolerances: relative=1e-08, absolute=1e-50, solution=1e-08

total number of linear solver iterations=5

total number of function evaluations=6

KSP Object: 1 MPI processes

type: gmres

GMRES: restart=30, using Classical (unmodified) Gram-Schmidt

GMRES: happy breakdown tolerance 1e-30

maximum iterations=10000, initial guess is zero

tolerances: relative=1e-05, absolute=1e-50, divergence=10000

left preconditioning

using PRECONDITIONED norm type for convergence test

# Sample output (PC and Mat)

PC Object: 1 MPI processes

type: lu

LU: out-of-place factorization

tolerance for zero pivot 2.22045e-14

matrix ordering: nd

factor fill ratio given 5, needed 2.95217

Factored matrix follows:

Matrix Object: 1 MPI processes

type: seqaij

rows=100, cols=100

package used to perform factorization: petsc

total: nonzeros=1358, allocated nonzeros=1358

total number of mallocs used during MatSetValues calls

not using I-node routines

linear system matrix = precondition matrix:

Matrix Object: 1 MPI processes

type: seqaij

rows=100, cols=100

total: nonzeros=460, allocated nonzeros=460

total number of mallocs used during MatSetValues calls =0

not using I-node routines

# In parallel

- ```
$ mpiexec -n 4  
./ex5 -da_grid_x 10 -da_grid_y 10 -par 6.7  
-snes_monitor -{ksp,snes}_converged_reason  
-snes_view -sub_pc_type lu
```
- How does the performance change as you
 - vary the number of processes (up to 32 or 64)?
 - increase the problem size?
 - try inexact subdomain solve?
 - try overlapping method: `-pc_type asm -pc_asm_overlap 2`
 - simulate a big machine: `-pc_asm_blocks 512`
 - change the Krylov method: `-ksp_type ibcgs`
 - use algebraic multigrid: `-pc_type hypre`
 - use smoothed aggregation multigrid: `-pc_type ml`

SNES ex62

Preconditioning

FEM Setup

```
./bin/pythonscripts/PetscGenerateFEMQuadrature.py  
2 2 2 1 laplacian  
2 1 1 1 gradient  
src/snes/examples/tutorials/ex62.h
```

SNES ex62

Preconditioning

Jacobi

ex62

```
-run_type full -bc_type dirichlet -show_solution 0  
-refinement_limit 0.00625 -interpolate 1  
-snes_monitor_short -snes_converged_reason  
  -snes_view  
-ksp_gmres_restart 100 -ksp_rtol 1.0e-9  
  -ksp_monitor_short  
-pc_type jacobi
```

SNES ex62

Preconditioning

Block diagonal

ex62

```
-run_type full -bc_type dirichlet -show_solution 0
-refinement_limit 0.00625 -interpolate 1
-snes_monitor_short -snes_converged_reason
  -snes_view
-ksp_type fgmres -ksp_gmres_restart 100
  -ksp_rtol 1.0e-9 -ksp_monitor_short
-pc_type fieldsplit -pc_fieldsplit_type additive
-fieldsplit_velocity_pc_type lu
-fieldsplit_pressure_pc_type jacobi
```

SNES ex62

Preconditioning

Block triangular

ex62

```
-run_type full -bc_type dirichlet -show_solution 0
-refinement_limit 0.00625 -interpolate 1
-snes_monitor_short -snes_converged_reason
  -snes_view
-ksp_type fgmres -ksp_gmres_restart 100
  -ksp_rtol 1.0e-9 -ksp_monitor_short
-pc_type fieldsplit -pc_fieldsplit_type multiplicati
-fieldsplit_velocity_pc_type lu
-fieldsplit_pressure_pc_type jacobi
```

SNES ex62

Preconditioning

Diagonal Schur complement

ex62

```
-run_type full -bc_type dirichlet -show_solution 0
-refinement_limit 0.00625 -interpolate 1
-snes_monitor_short -snes_converged_reason
  -snes_view
-ksp_type fgmres -ksp_gmres_restart 100
  -ksp_rtol 1.0e-9 -ksp_monitor_short
-pc_type fieldsplit -pc_fieldsplit_type schur
  -pc_fieldsplit_schur_factorization_type diag
-fieldsplit_velocity_ksp_type gmres
  -fieldsplit_velocity_pc_type lu
-fieldsplit_pressure_ksp_rtol 1e-10
  -fieldsplit_pressure_pc_type jacobi
```

SNES ex62

Preconditioning

Upper triangular Schur complement

ex62

```
-run_type full -bc_type dirichlet -show_solution 0
-refinement_limit 0.00625 -interpolate 1
-snes_monitor_short -snes_converged_reason
  -snes_view
-ksp_type fgmres -ksp_gmres_restart 100
  -ksp_rtol 1.0e-9 -ksp_monitor_short
-pc_type fieldsplit -pc_fieldsplit_type schur
  -pc_fieldsplit_schur_factorization_type upper
-fieldsplit_velocity_ksp_type gmres
  -fieldsplit_velocity_pc_type lu
-fieldsplit_pressure_ksp_rtol 1e-10
  -fieldsplit_pressure_pc_type jacobi
```

SNES ex62

Preconditioning

Lower triangular Schur complement

ex62

```
-run_type full -bc_type dirichlet -show_solution 0
-refinement_limit 0.00625 -interpolate 1
-snes_monitor_short -snes_converged_reason
  -snes_view
-ksp_type fgmres -ksp_gmres_restart 100
  -ksp_rtol 1.0e-9 -ksp_monitor_short
-pc_type fieldsplit -pc_fieldsplit_type schur
  -pc_fieldsplit_schur_factorization_type lower
-fieldsplit_velocity_ksp_type gmres
  -fieldsplit_velocity_pc_type lu
-fieldsplit_pressure_ksp_rtol 1e-10
  -fieldsplit_pressure_pc_type jacobi
```

SNES ex62

Preconditioning

Full Schur complement

ex62

```
-run_type full -bc_type dirichlet -show_solution 0
-refinement_limit 0.00625 -interpolate 1
-snes_monitor_short -snes_converged_reason
  -snes_view
-ksp_type fgmres -ksp_gmres_restart 100
  -ksp_rtol 1.0e-9 -ksp_monitor_short
-pc_type fieldsplit -pc_fieldsplit_type schur
  -pc_fieldsplit_schur_factorization_type full
-fieldsplit_velocity_ksp_type gmres
  -fieldsplit_velocity_pc_type lu
-fieldsplit_pressure_ksp_rtol 1e-10
  -fieldsplit_pressure_pc_type jacobi
```


User Projects

Create a new code based upon SNES Example 5.

1 Create a new directory

- `mkdir -p /home/knepley/proj/newsim/src`

2 Copy the source

- `cp ex5.c /home/knepley/proj/newsim/src`
- **Add `myStuff.c` and `myStuff2.F`**

3 Create a PETSc makefile

```
bin/ex5: src/ex5.o src/myStuff.o src/myStuff2.o
    ${CLINKER} -o $@ $^ ${PETSC_SNES_LIB}
include ${PETSC_DIR}/conf/variables
include ${PETSC_DIR}/conf/rules
```

To get the project ready-made

```
hg clone http://petsc.cs.iit.edu/petsc/tutorials/SimpleTutorial newsim
```